

Pulsed Latches Based Parallel Pipelined Architecture and Algorithm for Matrix Transposition

Shaheela A M¹, Anitta Antony²

¹ Student, M-tech in VLSI Design, ECE, IES College of Engineering, Chittilappilly, Kerala, India.

² Assistant Professor, Department of ECE, IES College of Engineering, Chittilappilly, Kerala, India.

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Abstract: This paper proposes a new algorithm and architecture for continuous flow matrix transposition using pulsed latches. The algorithm supports P-parallel matrix transposition. The hardware architecture reaches the theoretical minimum in terms of memory and latency. Low power consumption and area efficiency is the most advantage of using pulsed latches. Instead of using conventional single pulsed clock signals, here we use multiple non overlap delayed pulsed clock signals in order to reduce the timing problems between pulsed latches. Compared with the state-of-the-art architecture, the proposed architecture supports matrices whose rows and columns are integer multiples of P. Here P can be arbitrary, including but not limited to power-of-two-integers. More over our result provide additional insight into continuous flow non-square matrix transposition.

Key Word: Continuous flow; Matrix transposition; State-of-art architecture;

I. INTRODUCTION

A matrix is a square or rectangular array of numbers or functions that arranged in a fixed number of rows and columns. In Linear algebra, the transpose of a matrix is one of the most commonly used methods in matrix transformations. For a given matrix, the transpose of a matrix is obtained by interchanging rows into columns and columns to rows. The matrix transpose is denoted by the letter T. The application of matrix transposition is extravagant these days. In image signal processing, matrix transposition is used for adding brightness or applying filters or image rotation. As matrices are the fundamental concepts in AI, matrix transpose leads a major role in machine learning. As a key component in matrix-based algorithms, it plays an important role in deep learning applications, including computer vision and nature language processing. Specifically, matrix transpose operations are often implemented in fully connected layers, convolutional layers, and self-attention layers. To reduce the area and power consumption flip-flops are replaced with pulsed latches. This paper uses shift registers using pulsed latches instead of using master slave flip flops. Such a shift register using pulsed latches reduces the power consumption and area. The timing problem is solved by using multiple non-overlap delayed pulsed clock signals instead of the conventional single pulsed clock signal. The shift register used additional temporary storage latch.

II. LITERATURE SURVEY

The crucial role of matrix transpose in SAR (Synthetic Aperture Radar) imaging technique and introduced two new matrix transpose methods and implemented. Two algorithms namely Range-Doppler algorithm (RD) and Chirp-Scaling algorithm (CS) has introduced. Range-Doppler (RD) algorithm is the most effective and commonly used algorithm in SAR imaging technique. It splits two dimensional images to one dimensional processing. The main phases of RD algorithm is Preprocessing, Range compression, Matrix transpose and Azimuth compression. To the improvement of RD algorithm introduced CS (Chirp-Scaling) algorithm is introduced. CS algorithm maintains a good phase-precision by using a phase factor namely Chirp-Scaling factor. Chirp-Scaling factor is used to change the phase shift property of migration in order to avoid the interpolation operation. CS algorithm requires a Preprocessing, Azimuth FFT, Range FFT, Range IFFT and Azimuth IFF.[1]

The bit reversal on series of data and took simple and optimum circuits. Simple in the sense it consisted of only buffers and multiplexers and optimum in two senses: first it uses only minimum number of registers that are necessary for calculating bit reversal and the second one is minimum latency. The circuit is made optimum in two senses: minimum latency and minimum storage elements. The output frequencies of the FFT are sorted out in pipelined architecture as the circuits are optimum for that functioning. Optimum circuits have been found out.[17]

A pipelined algorithm and architecture for finding out the transpose of N x N matrix. It uses registers and gives minimum memory and latency. The circuit has a simple control strategy and is a identical cascaded basic circuit. It can be only applicable for square matrix. Matrix transposition is a simple operation that can be expressed as

$$A_{i,j} = A_{j,i} \text{ for all, } i, j = 0, 1, 2, \dots, N-1.$$

Consider an N x N matrix and its transposed matrix. The matrix transposition can be found out by reversing the elements on every diagonal from the bottom left to the top right. We can employ a series of steps and permutations among elements on each diagonal to achieve this reversal. Based on the above considerations, we present a pipelined matrix transposition algorithm. Modular pipelined architecture is introduced and is achieved by series of permutations namely Basic permutation circuit and Cascade transposition architecture. In basic permutation circuit, the bit reversal is done by swapping the position of two elements with a fixed interval. And in cascaded transposition architecture composed of N - 1 cascade basic

permutation circuits with a shift register (SR) of length $N-1$. It includes only identical circuits. [8]

A unique pipelined algorithm for transposing non-square matrices and describe the corresponding architecture for this algorithm. This architecture composed of series of cascaded basic circuit and is controlled by control strategy. The proposed architecture and algorithm. Besides, the proposed calculation and engineering could be handily reached out to N -equal executions for lattice interpretation. This architecture upholds lattices whose lines and segments are number products; it is essentially utilized for radix-2s butterfly calculations utilizing lattice interpretations. Trial results show that the proposed single-way design can diminish the calculation cycles and circuit region by an element of 9.18% and 5.87%, respectively, for a 32×16 lattice interpretation calculation, looked at with those of an as of late proposed best in class engineering for grid interpretation. Matrix transposition is a fundamental operation that can be expressed as

$$A_{i,j} = (A^T)_{j,i}, \text{ where } i = 0, 1, 2, \dots, N_R - 1 \text{ and } j = 0, 1, 2, \dots, N_C - 1.$$

Two methods are taken into consideration Basic serial exchange circuit and cascade transposition architecture. In basic serial exchange circuit Garrido et al proposed a piece inversion circuit that can trade the places of two components with a decent stretch between them, where S and S^- represent the control flags that can be utilized to change the status of the two multiplexers in the circuit to one or the other pass-by or trade modes; what's more, L alludes to the length of the cushion utilized for component trading.

If a matrix has $N_R \times N_C$ number of rows and columns respectively, the transposition architecture composed of $N-1$ cascaded permutation. The proposed $N_R \times N_C$ lattice interpretation engineering is made out of $N-1$ fountain fundamental change circuits with a shift register (SR) of length $N-1$ and $(K-1)(N-1)$ overflow fundamental change circuits with a SR of length N . Altogether, the proposed overflow interpretation architecture is created of $K(N-1)$ overflow fundamental change circuits. It is extended up to N parallel matrix and also supports continuous data, and is suitable for realizing pipelined multi-dimensional FHT and FFT operations. Image processing and transposition of non-square matrix is found out here.[12]

III. EXISTING SYSTEM

The existing system is to find the matrix transposition in a parallel and pipelined manner using registers consisting of flip flops. The transpose of any matrix such as square or non-square matrix can be found out using this. It is a basic pipelined algorithm and can be used to find p parallel matrix transposition. The transposition is found in 3 steps. Step A B & C.

This architecture is meant for P -parallel matrix transposition. The matrix transposition is calculated by a set of basic permutations along with a circuit and a set of algorithms in a single path way. Cascaded P -parallel architecture and is controlled by control strategy. Memory and latency is also take into consideration. Cascaded P -architecture involves two PEs. PE_1 and PE_{II} . The proposed architecture composed of shift registers cascaded serially to perform p -parallel permutations. The function of PE_1 is to exchange data points between different input ports and it completes step B. Step A & C is completed by PE_{II} architecture where, data points are exchanged same input ports but in different clock cycles.

Several counters control the control strategy of above architecture. The control signals are denoted by S_n where, n is the number of stages in step A, B & C. The control signals are generated by three counters, called C_0, C_1 and C_2 . The control strategies in each steps are: In Step A, $n \in [0, (n_c - 1)(P - 1) - 1]$, S_n as follows:

$$S_n = 1 \text{ } LOC_1 \leq C_0 \leq LOC_1 + (offset_1 - 1, 0 \text{ else.}$$

In Step B, $n \in [0, P - 2]$, S_n as follows:

$$S_n = 1 \text{ } 1 \leq C_1 \leq P - n - 1, 0 \text{ else.}$$

In Step C, $n \in [0, ((n_r - 1)(n_c P - 1) - 1]$, S_n as follows:

$$S_n = 1 \text{ } LOC_2 \leq C_2 \leq LOC_2 + offset_2 - 1, 0 \text{ else.}$$

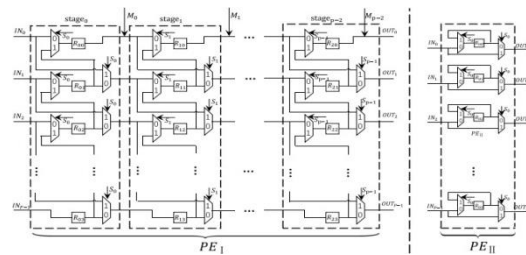


Fig 3.1 P-parallel Pes in algorithm 1

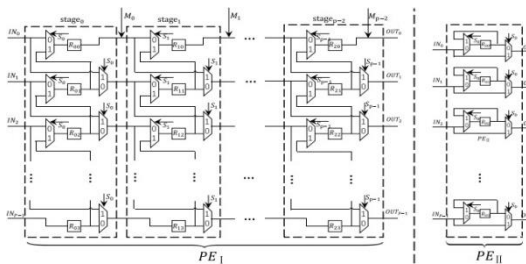


Fig 3.2 P-parallel architecture block diagram

Considering a $N_R \times N_C$ matrix, the number of $stage_1$ in step A is $(n_c - 1) \times (P - 1)$, the number of $stage_2$ in step B is

$P - 1$, the number of $stage_3$ in step C is $(n_C P - 1) \times (n_r - 1)$; so, the total size of the memory is as follows:

$$\begin{aligned} D &= (n_c - 1) \times (P - 1) \times P + (P - 1) \times P + (n_c P - 1) \times (n_r - 1) \times P, \\ &= (n_c P - 1)(n_r P - 1) + P - 1, \\ &= (N_C - 1)(N_R - 1) + P - 1 \end{aligned}$$

and the total latency is as follows:

$$L = D/P, = [(N_C - 1)(N_R - 1) + P - 1]/P.$$

This architecture achieves a minimum latency and memory. This proposed architecture uses more multiplexers than others to support P-parallel matrix algorithm for any square and non-square matrix transposition. The control strategy used here is somehow easy to implement and execute.

IV. PROPOSED ARCHITECTURE

A low power and area efficient pulsed latches is proposed in this paper instead of flip flops that takes a larger area and consumes high power. By using pulsed latches timing problems may happen in the entire circuitry. So, in order to avoid that uses multiple non-overlapped delayed pulse clock signals instead of using conventional single pulsed clock signals. Additional temporary storage latches are included. Master slave flip flop contacting two latched is being replaced by a pulsed latch consisting of pulsed clock signals as shown in Fig 4.1. By using this method, the required area and power consumption become half and it became low power and area efficient design procedure. Pulsed latches have timing problems inbuilt so, it cannot be used directly in shift registers.

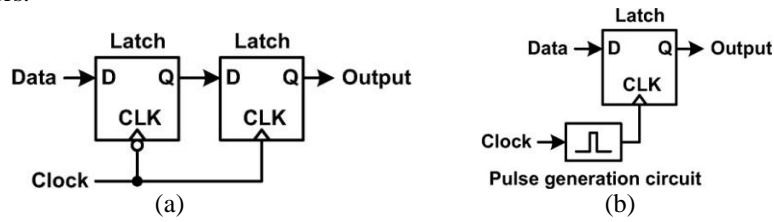


Fig 4.1 (a) Master slave flip flop (b) pulsed latches.

A shift register is proposed which is divided into M sub shift registers in order to reduce the number of delayed pulsed clock signals. This delayed pulsed clock signals are generated by delayed pulsed clock generator. For better understanding, a 4-bit sub shift register consists of 5 latches in which the 4 latches store 4-bit data and last latch store 1-bit temporary data. Here 5 non-overlap delayed pulsed clock signals are generated

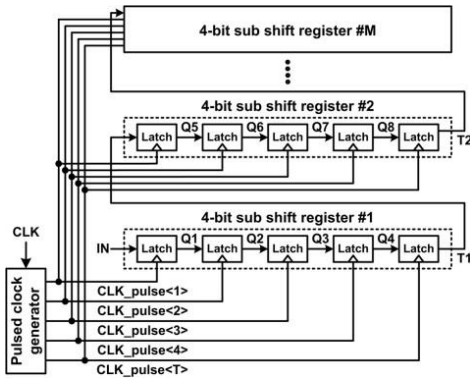


Fig 4.2 schematic of proposed shift register

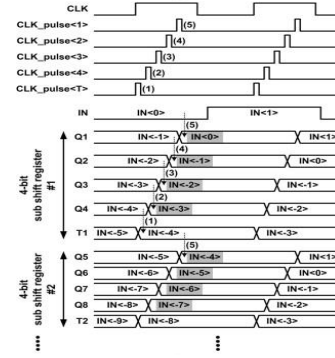


Fig 4.3 waveform of proposed shift register

The proposed shift register used delayed pulsed clock generator which uses an extra AND gate than conventional delayed pulsed clock generator. But in conventional delayed pulsed clock generator, the width of the clock pulse is larger than the summation of raising and falling times in delay circuits to keep the shape. However, the clock width is comparatively shorter in delayed pulsed clock generator since the sharp pulse clock signal is generated by the AND gate and two delayed signals. The power and area optimization goes hand in hand. The power is mainly consumed by latches for data transition and clock loading and the total area of utilization also depends on clock loading of latches.

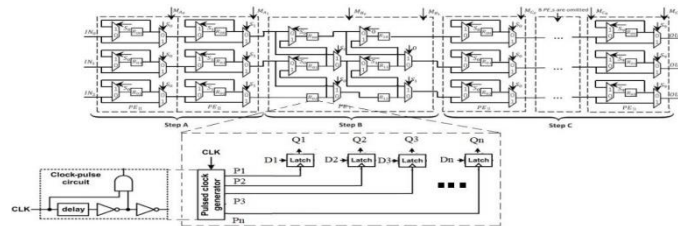


Fig 4.4 Proposed matrix transposition model using pulsed latches and delayed pulsed clock generator.

V. EXPERIMENTAL RESULTS

The proposed matrix transposition architecture is simulated on the ModelSim software tool. The existing and proposed architectures are evaluated in the FPGA Xilinx 14.4 ISE tool. It is analyzed in a system consisting of Intel i5 processor with 8 GB of RAM and 500 GB harddisk.

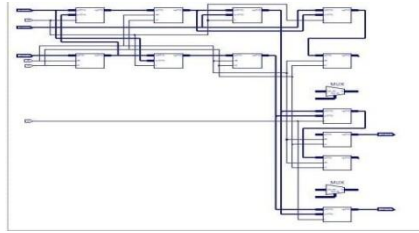


Fig 5.1 RTL view of PE I algorithm.

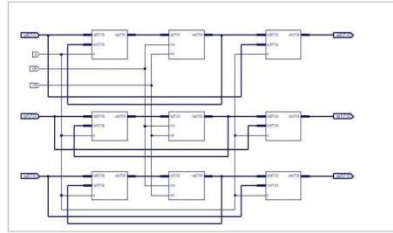


Fig 5.2 RTL view of PE II algorithm.

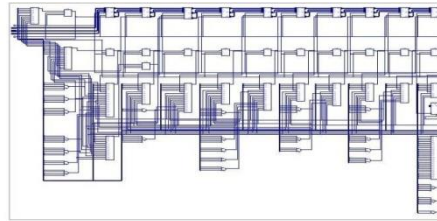


Fig 5.3 RTL view of 9 X 6 matrix

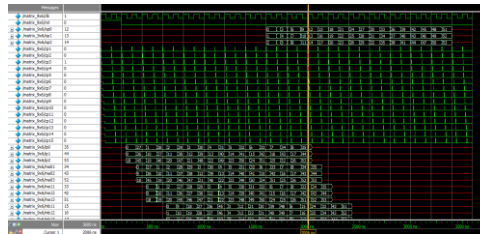


Fig 5.4 Output timing diagram of 9 X 6 matrix

VI. COMPARATIVE ANALYSIS

The proposed system comes with an effective area, low power consumption and the delay element is also low. Comparing the existing and proposed system in terms of area, power and delay

Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
Number of Slice Flip Flops	435	13,824	3%	
Number of 4 input LUTs	1,409	13,824	10%	
Logic Distribution				
Number of occupied Slices	778	6,912	11%	
Number of Slices containing only related logic	778	6,912	100%	
Number of Slices containing unrelated logic	0	778	0%	
Total Number 4 input LUTs	1,444	13,824	10%	
Number used as logic	1,409			
Number used as a route-thru	35			
Number of bonded IOBs	25	510	4%	
Number of Block RAMs	3	72	4%	
Number of GCLXs	1	4	25%	
Number of GCLXIOBs	1	4	25%	
Total equivalent gate count for design	61,611			
Additional JTAG gate count for IOBs	1,248			
Performance Summary				
Final Timing Score:	0	Pinout Data:	Pinout Report	
Routing Results:	All Signals Completely Routed	Clock Data:	Clock Report	
Timing Constraints:	All Constraints Met			

(a)

Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
Number of Slice Flip Flops	402	13,824	2%	
Number of 4 input LUTs	1,064	13,824	7%	
Logic Distribution				
Number of occupied Slices	568	6,912	8%	
Number of Slices containing only related logic	568	6,912	100%	
Number of Slices containing unrelated logic	0	568	0%	
Total Number 4 input LUTs	1,099	13,824	7%	
Number used as logic	1,064			
Number used as a route-thru	35			
Number of bonded IOBs	25	510	4%	
Number of Block RAMs	3	72	4%	
Number of GCLXs	2	4	50%	
Number of GCLXIOBs	1	4	25%	
Total equivalent gate count for design	59,148			
Additional JTAG gate count for IOBs	1,248			
Performance Summary				
Final Timing Score:	0	Pinout Data:	Pinout Report	
Routing Results:	All Signals Completely Routed	Clock Data:	Clock Report	
Timing Constraints:	All Constraints Met			

(b)

Fig 6.1 Area utilization summary (a) existing system (b) proposed system.

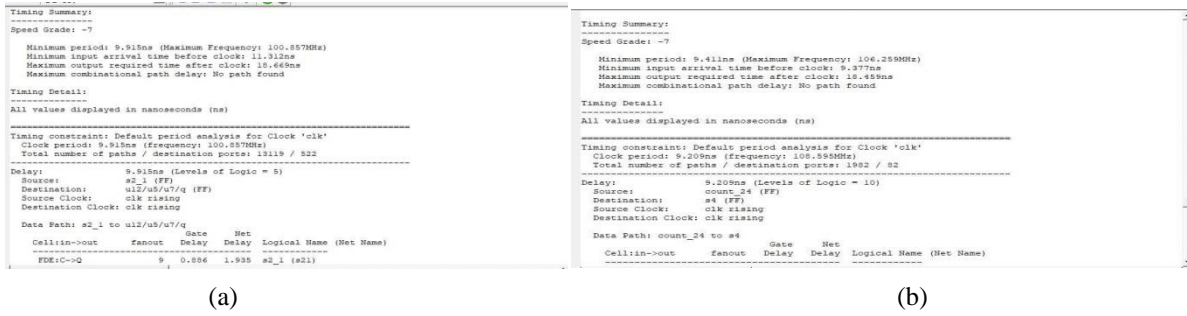


Fig 6.2 Delay analysis of (a) existing system (b) proposed system.

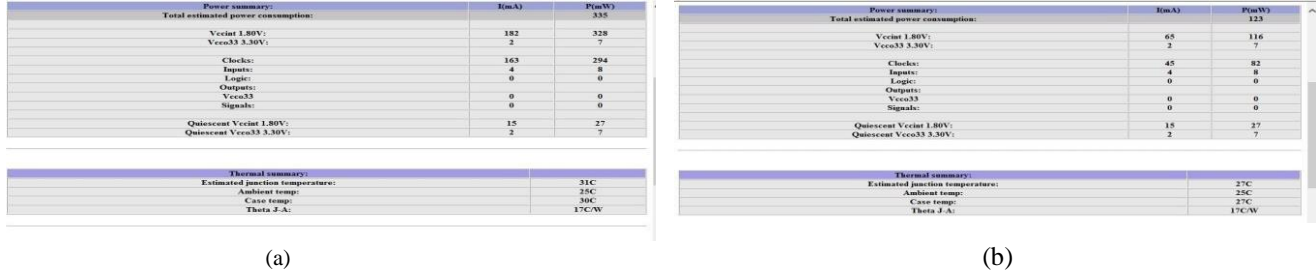


Fig 6.3 Power Comparison of (a) Existing system (b) proposed system.

VII.CONCLUSION

Transpose of a matrix is performed in a circuit consisting of pulsed latches in which the clock pulse is generated by delayed pulsed clock generator. The newly proposed circuit gives a low power and area efficient design. The delay problems occurring in the pulsed latches normally is kick stopped by using delayed pulsed clock generator instead of conventional clock pulse generator. Multiple non-overlapped delayed pulsed clock generators are used. The latches are grouped for generating a small number of pulsed clock to several sub shift registers and by using additional latches for temporary data storage.

The transposition of continuous flow matrix is found out. Here, P-parallel architecture is used to find the transpose of any row and column matrix. The architecture gives a theoretical minimum in terms of memory and latency.

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